

Worksheet 7-6: Factoring Trinomials

**For a trinomial of the form $x^2 + bx + c$,
the factors are of the form $(x + m)(x + n)$, where $m + n = b$ and $mn = c$.**

Therefore:

$$x^2 + bx + c = x^2 + (m + n)x + (mn) = (x + m)(x + n)$$

To factor a trinomial means writing $x^2 + bx + c$ as $(x + m)(x + n)$.

How do we find m and n to factor the trinomial?

We need to find two factors when multiplied equals c but added to b .

Example 1:

Factor each trinomial.

(Hint: Find two factors of c when added together equals b . **Watch for the signs!**)

(a)	$x^2 + 5x + 6$	$b = 5$	$c = 6$	$m = 2$	$n = 3$	x^2 6
	$= (x + 2)(x + 3)$		$2 \times 3 = 6$	$2 + 3 = 5$		x 2
						x 3

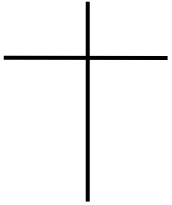
(Check your answer by expanding the brackets to see if the brackets multiplied to $x^2 + 5x + 6$.)

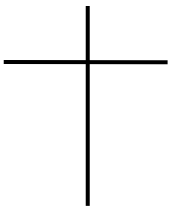
(b)	$a^2 - 3a - 18$	$b = -3$	$c = -18$	$m = -6$	$n = 3$	a^2 -18
	$= (a - 6)(a + 3)$		$-6 \times 3 = -18$	$-6 + 3 = -3$		a -6
						a 3

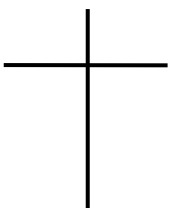
(c)	$y^2 - 8y + 15$	$b = -8$	$c = 15$	$m = -3$	$n = -5$	y^2 15
	$= (y - 3)(y - 5)$		$-3 \times -5 = 15$	$-3 + -5 = -8$		y -3
						y -5

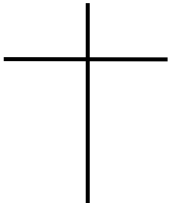
When c is **positive** then the signs of m and n must both be either positive or negative... $++ / -- \rightarrow +$
then $m \times n = c$ and $|m| + |n| = b$ with the signs of m and $n =$ the sign of b (**b determines the signs**)

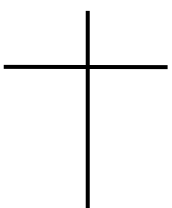
When c is **negative** then the signs of m and n must be one positive and one negative... $+ - / - + \rightarrow -$
then $m \times n = c$ and $|m| - |n| = b$ with the sign of $b =$ the sign of $|m|$ or $|n|$ whichever is greater

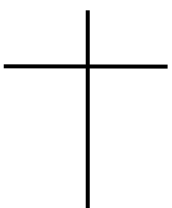
1. Factor $x^2 + 6x + 8$. $b =$ $c =$ $m =$ $n =$ 

2. Factor $a^2 - 13a + 36$. $b =$ $c =$ $m =$ $n =$ 

3. Factor $y^2 - 2y - 24$. $b =$ $c =$ $m =$ $n =$ 

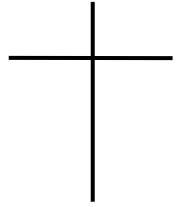
4. Factor $x^2 + 7x + 12$. $b =$ $c =$ $m =$ $n =$ 

5. Factor $a^2 - 9a + 18$. $b =$ $c =$ $m =$ $n =$ 

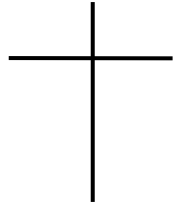
6. Factor $y^2 + 7y - 18$. $b =$ $c =$ $m =$ $n =$ 

Worksheet 7-7: Factoring Trinomials in the form $x^2 + bx + c$

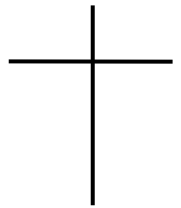
1. Factor $x^2 + 13x + 12$. $b =$ $c =$ $m =$ $n =$



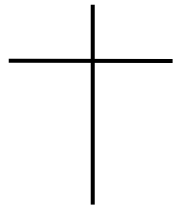
2. Factor $a^2 - 8a + 15$. $b =$ $c =$ $m =$ $n =$



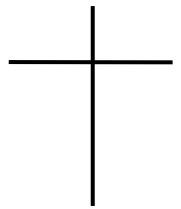
3. Factor $y^2 - 7y - 30$. $b =$ $c =$ $m =$ $n =$



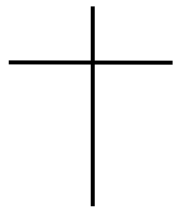
4. Factor $x^2 + 11x + 28$. $b =$ $c =$ $m =$ $n =$



5. Factor $a^2 - 11a + 24$. $b =$ $c =$ $m =$ $n =$

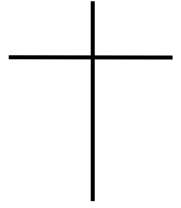


6. Factor $y^2 + 2y - 35$. $b =$ $c =$ $m =$ $n =$

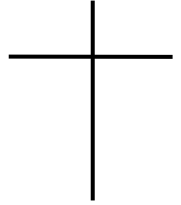
**Answers:** 1. $(x+1)(x+12)$; 2. $(a-3)(a-5)$; 3. $(y+3)(y-10)$; 4. $(x+4)(x+7)$; 5. $(a-3)(a-8)$; 6. $(y-5)(y+7)$

****IMPORTANT NOTE:** $(x+a)(x+a) = (x+a)^2$ and $(x-a)(x-a) = (x-a)^2$ **

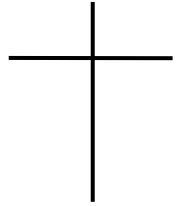
7. Factor $x^2 + 14x + 49$. $b =$ $c =$ $m =$ $n =$



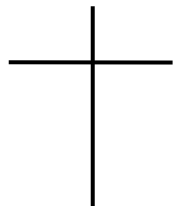
8. Factor $a^2 - 10a + 25$. $b =$ $c =$ $m =$ $n =$



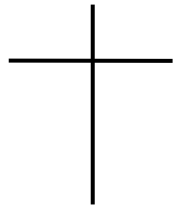
9. Factor $y^2 + 8y + 16$. $b =$ $c =$ $m =$ $n =$



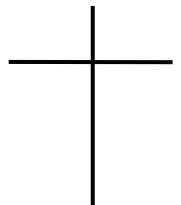
10. Factor $x^2 - 2x + 1$. $b =$ $c =$ $m =$ $n =$



11. Factor $a^2 - 4$. $b = 0$ $c =$ $m =$ $n =$



12. Factor $y^2 - 64$. $b =$ $c =$ $m =$ $n =$



Answers: 7. $(x+7)^2$; 8. $(a-5)^2$; 9. $(y+4)^2$; 10. $(x-1)^2$; 11. $(a+2)(a-2)$; 12. $(y+8)(y-8)$

Bingo: Factoring Trinomials

Factor.

1. $x^2 + 12x + 32$

2. $y^2 - 4y - 45$

3. $a^2 - 17a + 70$

4. $x^2 + x - 72$

5. $y^2 - 4y + 4$

6. $a^2 + 6a + 9$

7. $x^2 - 18x + 81$

8. $y^2 - 121$

9. $a^2 - 36$

+	+	+
+	+	+
+	+	+